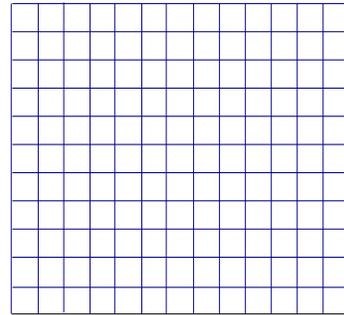


DIRECTIONS To receive full credit, you must provide complete legible solutions to the following problems in the space provided. No Attached papers. Transfer all your answers to the space provided.

1. Consider the given vector equation. $\mathbf{r}(t) = 3\sin(t)\mathbf{i} - 2\cos(t)\mathbf{j}$, $t = 3\pi/4$

a. Find $\mathbf{r}'(t)$. Ans _____

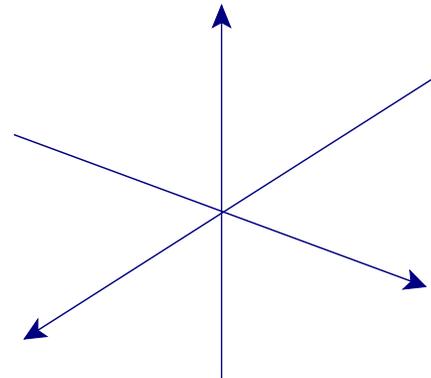
b. Sketch the plane curve together with the position vector $\mathbf{r}(t)$ and the tangent vector $\mathbf{r}'(t)$ for the given value of t .



2. Consider the given vector equation $\mathbf{r}(t) = 2\sin t\mathbf{i} + 2\cos t\mathbf{j} + t\mathbf{k}$, $t = \pi$

a. Find $\mathbf{r}'(t)$. Ans _____

b. Sketch the plane curve together with the position vector $\mathbf{r}(t)$ and the tangent vector $\mathbf{r}'(t)$ for the given value of t .



3. Find parametric equations for the tangent line to the helix with parametric equations $x = 5\cos(t)$, $y = 3\sin(t)$, $z = t$ at the point $(0, 3, \pi/2)$.

Ans _____

4. If $\mathbf{r}(t) = 4t\mathbf{i} + 6t^2\mathbf{j} + 6t^3\mathbf{k}$, find $\mathbf{T}(1)$ Ans _____
a. $\mathbf{T}(1)$ Ans _____

b. $\mathbf{r}'(t) \times \mathbf{r}''(t)$ Ans _____

4. Evaluate the integral. Ans _____
$$\int_0^1 \left(\frac{5}{1+t^2} \mathbf{j} + \frac{3t^2}{1+t^3} \mathbf{k} \right) dt$$

5. Find $\mathbf{r}(t)$ if $\mathbf{r}'(t) = t^5\mathbf{i} + e^t\mathbf{j} + 2te^{2t}\mathbf{k}$ and $\mathbf{r}(0) = \mathbf{i} + \mathbf{j} + \mathbf{k}$.
Ans _____

6. If $\mathbf{u}(t) = \langle \sin 6t, \cos 4t, t \rangle$ and $\mathbf{v}(t) = \langle t, \cos 4t, \sin 6t \rangle$
a. $\frac{d}{dt}(\mathbf{u}(t) \cdot \mathbf{v}(t))$ Ans _____

b. $\frac{d}{dt}(\mathbf{u}(t) \times \mathbf{v}(t))$ Ans _____